Package: MRReg (via r-universe)

March 6, 2025

Title MDL Multiresolution Linear Regression Framework

Version 0.1.5

Maintainer Chainarong Amornbunchornvej <grandca@gmail.com>

Description We provide the framework to analyze multiresolution partitions (e.g. country, provinces, subdistrict) where each individual data point belongs to only one partition in each layer (e.g. i belongs to subdistrict A, province P, and country Q). We assume that a partition in a higher layer subsumes lower-layer partitions (e.g. a nation is at the 1st layer subsumes all provinces at the 2nd layer). Given N individuals that have a pair of real values (x,y) that generated from independent variable X and dependent variable Y. Each individual i belongs to one partition per layer. Our goal is to find which partitions at which highest level that all individuals in the these partitions share the same linear model Y=f(X) where f is a linear function. The framework deploys the Minimum Description Length principle (MDL) to infer solutions. The publication of this package is at Chainarong Amornbunchornvej, Navaporn Surasvadi, Anon Plangprasopchok, and Suttipong Thajchayapong (2021) <doi:10.1145/3424670>.

License MIT + file LICENSE

URL https://github.com/DarkEyes/MRReg

BugReports https://github.com/DarkEyes/MRReg/issues Encoding UTF-8 LazyData false Depends R (>= 3.5.0), caret Imports igraph Roxygen list(markdown = TRUE) Suggests knitr, rmarkdown, markdown VignetteBuilder knitr RoxygenNote 7.1.2 Config/pak/sysreqs libglpk-dev libicu-dev libxml2-dev Repository https://darkeyes.r-universe.dev RemoteUrl https://github.com/darkeyes/mrreg RemoteRef HEAD RemoteSha 23a8d7ea2f999cf07c355746b014f621a81dd7be

Contents

FindMaxHomoOptimalPartitions	2
linearModelTraining	4
plotOptimalClustersTree	5
PrintOptimalClustersResult	6
SimpleSimulation	6
	~
	8

FindMaxHomoOptimalPartitions

FindMaxHomoOptimalPartitions

Description

FindMaxHomoOptimalPartitions is a main function for inferring optimal homogeneous clusters from a multiresolution dataset DataT.

Usage

Index

```
FindMaxHomoOptimalPartitions(
   DataT,
   gamma = 0.05,
   insigThs = 1e-08,
   alpha = 0.05,
   minInvs = 99,
   polyDegree = 1,
   expFlag = FALSE,
   messageFlag = FALSE
```

)

Arguments

contains a multiresolution dataset s.t. DataT\$X[i,d] is a value of feature d of individual i, DataT\$Y[i] is value of target variable of individual i that we want to fit DataT\$Y ~ DataT\$X in linear model, and clsLayer[i,j] is a cluster ID of individual i at layer j; clsLayer[i,1] is the first layer that everyone typically belongs to a single cluster.
is a threshold to

insigThs	is a threshold to determine whether a magnitude of a feature coefficient is enough so that the feature is designated as a selected feature.
alpha	is a significance level to determine whether a magnitude of a feature coefficient is enough so that the feature is designated as a selected feature.
minInvs	is a minimum number of individuals for a cluster to be considered for inferring $eta(C)cv$, otherwise, $eta(C)cv=0$.
polyDegree	is a degree of polynomial function that is used to fit the data. If it is greater than 1, the polynomial formula is used in $lm()$ instead of "y=.".
expFlag	is an exponential flag to control the formula for data fitting. If it is true, then the $exp()$ formula is used in $lm()$ instead of "y=.".
messageFlag	is a flag. If it is true, the function shows the text regarding the progress of computing.

Value

This function returns Copt, models, nNodes, invOptCls, and minR2cv.

Copt	Copt[p,1] is equal to k implies a cluster that is a pth member of the maxi- mal homogeneous partition is at kth layer and the cluster name in kth layer is Copt[p,2]Copt[p,3] is "Model Information Reduction Ratio" I({C},H0,Hlin)
	of pth member of the maximal homogeneous partition: positive means the linear
	model is better than the null model. Lastly, Copt $[p, 4]$ is the squared correlation between predicted and real V in CV step ($eta(C)ev$) of pth member of the max
	imal homogeneous partition. The greater Copt[p,4], the higher homogeneous degree of this cluster.
clustInfoRecRatio	
	<pre>models[[k]][[j]]\$clustInfoRecRatio is the "Cluster Information Reduc- tion Ratio" I(Cj,Cjchildren,H) between the jth cluster in kth layer and its children clusters in (k+1)th layer: positive means current cluster is better than its children clusters. Hence, we should keep this cluster at the member of maxi- mal homogeneous partition instead of its children.</pre>
models	models[[j]][[k]] is a linear model of a cluster ID k at the layer j. The $models[[j]][[k]]$ \$selFeatureSet represents a set of selected-feature indices of the model where the feature index 1 is the intercept, and the feature index d is the (d-1)th variable DataT\$X[,d-1].
invOptCls	<pre>invOptCls[i,1] is the layer of optimal cluster of individual i. The optimal cluster of i is invOptCls[i,2].</pre>
minR2cv	is the value of $eta(C)cv$ from the cluster that has the lowest $eta(C)cv$.
DataT	is an updated DataT with the helper variables for plotting and printing results.

Examples

Running FindMaxHomoOptimalPartitions using simulation data DataT<-SimpleSimulation(100,type=1) obj<-FindMaxHomoOptimalPartitions(DataT,gamma=0.05)</pre> linearModelTraining linearModelTraining

Description

linearModelTraining is a support function for training linear models for partitions in all layers.

Usage

```
linearModelTraining(
  DataT,
  insigThs = 1e-08,
  alpha = 0.05,
  messageFlag = FALSE,
  polyDegree = 1,
  expFlag = FALSE
)
```

Arguments

DataT	contains a multiresolution dataset s.t. DataT\$X[i,d] is a value of feature d of individual i, DataT\$Y[i] is value of target variable of individual i that we want to fit DataT\$Y ~ DataT\$X in linear model, and clsLayer[i,j] is a cluster ID of individual i at layer j; clsLayer[i,1] is the first layer that everyone typically belongs to a single cluster.
insigThs	is a threshold to determine whether a magnitude of a feature coefficient is enough so that the feature is designated as a selected feature.
alpha	is a significance level to determine whether a magnitude of a feature coefficient is enough so that the feature is designated as a selected feature.
messageFlag	is a flag. If it is true, the function shows the text regarding the progress of computing.
polyDegree	is a degree of polynomial function that is used to fit the data. If it is greater than 1, the polynomial formula is used in $lm()$ instead of "y=.".
expFlag	is an exponential flag to control the formula for data fitting. If it is true, then the $exp()$ formula is used in $lm()$ instead of "y=.".

Value

This function returns models and DataT.

models	<pre>models[[j]][[k]] is a linear model of a cluster ID k at the layer j. The models[[j]][[k]]\$selFeatureSet represents a set of selected-feature indices of the model where the feature index 1 is the intercept, and the feature index d is the (d-1)th variable DataT\$X[,d-1].</pre>
DataT	is a DataT with DataT $nNodes,$ which is a number of total models from all layers.

plotOptimalClustersTree

Examples

```
# Running linearModelTraining using simulation data
DataT<-SimpleSimulation(100,type=1)
obj<-linearModelTraining(DataT)</pre>
```

plotOptimalClustersTree

plotOptimalClustersTree

Description

plotOptimalClustersTree is a support function for plotting the hierarchical tree of optimal clusters from FindMaxHomoOptimalPartitions function.

The red node(s) are the optimal homogeneous clusters while the gray nodes are non-optimal clusters.

Usage

```
plotOptimalClustersTree(resObj)
```

Arguments

res0bj is an object list, which is the output of FindMaxHomoOptimalPartitions function

Value

No return value, called for plotting the hierarchical tree of optimal clusters.

Examples

```
# Running FindMaxHomoOptimalPartitions using simulation data
DataT<-SimpleSimulation(100,type=1)
obj<-FindMaxHomoOptimalPartitions(DataT,gamma=0.05)
# Plotting the result
plotOptimalClustersTree(obj)</pre>
```

PrintOptimalClustersResult

PrintOptimalClustersResult

Description

PrintOptimalClustersResult is a support function for printing the optimal clusters from FindMax-HomoOptimalPartitions function.

Usage

```
PrintOptimalClustersResult(resObj, selFeature = FALSE)
```

Arguments

resObj	is an object list, which is the output of FindMaxHomoOptimalPartitions function
selFeature	is a flag. If it is true, then the function shows the selected feature(s) of each optimal cluster.

Value

No return value, called for printing optimal clusters.

Examples

```
# Running FindMaxHomoOptimalPartitions using simulation data
DataT<-SimpleSimulation(100,type=1)
obj<-FindMaxHomoOptimalPartitions(DataT,gamma=0.05)
# Printing the result
PrintOptimalClustersResult(obj)
```

SimpleSimulation SimpleSimulation

Description

SimpleSimulation is a support function for generating multiresolution datasets.

All simulation types have three layers except the type 6 has four layers.

The type-1 simulation has all individuals belong to the same homogeneous partition in the first layer.

The type-2 simulation has four homogeneous partitions in a second layer. Each partition has its own models.

The type-3 simulation has eight homogeneous partitions in a third layer. Each partition has its own models

SimpleSimulation

The type-4 simulation has one homogeneous partition in a second layer, four homogeneous partitions in a third layer, and eight homogeneous partitions in a fourth layer. Each partition has its own model.

The type-5 simulation is similar to type-4 simulation but Y=h(X) is an exponential function.

The type-6 simulation is similar to type-4 simulation but Y=h(X) is a polynomial function with degree parameter.

Usage

```
SimpleSimulation(indvN = 10000, type = 1, degree = 2)
```

Arguments

ind∨N	is a number of individuals per homogeneous partition.
type	is a type of simulation dataset. There are four types.
degree	is a degree parameter of a polynomial function for type-5 simulation

Value

The function returns a multiresolution dataset.

DataT\$X[i,d]	is a value of feature d of individual i
DataT\$Y[i]	is value of target variable of individual i that we want to fit DataT\$Y ~ DataT\$X in linear model
clsLayer[i,j]	is a cluster ID of individual i at layer j; clsLayer[i,1] is the first layer that everyone typically belongs to a single cluster.
DataT\$TrueFeature[i]	
	is equal to d if a true feature is DataT\$X[i,d-1] that DataT\$Y[i] is dependent with. Note that d = 1 is reserved for the intercept value in a linear model.

Examples

Running SimpleSimulation to generate a dataset. DataT<-SimpleSimulation(100,type=1)</pre>

Index

 ${\tt FindMaxHomoOptimalPartitions, 2}$

linearModelTraining, 4

plotOptimalClustersTree, 5
PrintOptimalClustersResult, 6

 $\texttt{SimpleSimulation}, \mathbf{6}$